

# BSEH Practice Paper (March 2024)

(2023-24)

## Marking Scheme

### MATHEMATICS

**SET-B**  
**CODE: 835**

⇒ Important Instructions: • All answers provided in the Marking scheme are SUGGESTIVE  
• Examiners are requested to accept all possible alternative correct answer(s).

SECTION – A (1Mark × 20Q)		
Q. No.	EXPECTED ANSWERS	Marks
Question 1.	Let R be the relation in the set N given by $R = \{(a, b) : b = a + 1, b > 5\}$ . Choose the correct answer.	
<b>Solution:</b>	(B) $(7, 8) \in R$	1
Question 2.	$\cos^{-1}(\cos \frac{7\pi}{6})$ is equal to	
<b>Solution:</b>	(B) $\frac{5\pi}{6}$	1
Question 3.	If $A = \begin{bmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{bmatrix}$ , then $A'A$ is:	
<b>Solution:</b>	(A) I	1
Question 4.	If A and B are invertible matrices, then which of the following is not correct	
<b>Solution:</b>	(D) $(A + B)^{-1} = B^{-1} + A^{-1}$	1
Question 5.	If the vertices of a triangle are $(-2, -3)$ , $(3, 2)$ and $(-1, -8)$ , then by using determinants its area is	
<b>Solution:</b>	(A) 15	1
Question 6.	If $y = \log x^2$ , then $\frac{d^2y}{dx^2}$ is equal to :	
<b>Solution:</b>	(A) $\frac{-2}{x^2}$	1
Question 7.	The antiderivative of $(1 - x)\sqrt{x}$ equals:	
<b>Solution:</b>	(B) $\frac{2}{3}x^{\frac{3}{2}} - \frac{2}{5}x^{\frac{5}{2}} + C$	1
Question 8.	$\int e^x \sec x (1 + \tan x) dx$ equals	
<b>Solution:</b>	(C) $e^x \sec x + C$	1
Question 9.	The value of $\int_{-\pi/2}^{\pi/2} \tan^5 x dx$ is	
<b>Solution:</b>	(C) 0	1
Question 10.	The degree of the differential equation $(\frac{d^2y}{dx^2})^3 + (\frac{dy}{dx})^2 + \sin(\frac{dy}{dx}) + 1 = 0$ is :	

<b>Solution:</b>	(D) not defined	1
Question 11.	How many number of arbitrary constants are there in the general solution of a differential equation of fourth order?	
<b>Solution:</b>	<b>4</b>	1
Question 12.	The function $f(x) = \begin{cases} \frac{\sin x}{x} + \cos x, & \text{if } x \neq 0 \\ k, & \text{if } x = 0 \end{cases}$ is continuous at $x = 0$ , then find the value of k	
<b>Solution:</b>	$\lim_{x \rightarrow 0} f(x) = \lim_{x \rightarrow 0} \left( \frac{\sin x}{x} + \cos x \right)$ $= 1 + 1$ $= 2$ <p>Since <math>f(x)</math> is continuous at <math>x = 0</math></p> $\therefore \lim_{x \rightarrow 0} f(x) = f(0)$ $\Rightarrow 2 = k$	1
Question 13.	If a line makes angles $90^\circ, 135^\circ, 45^\circ$ with the x, y and z-axes respectively, find its direction cosines.	
<b>Solution:</b>	<p>Line makes angles <math>90^\circ, 135^\circ, 45^\circ</math> with the x,y and z-axes respectively</p> <p><math>\therefore</math> Direction Cosines are</p> $l = \cos 90^\circ, m = \cos 135^\circ, n = \cos 45^\circ$ $l = 0, m = \frac{-1}{\sqrt{2}}, n = \frac{1}{\sqrt{2}}$ <p><math>\Rightarrow</math> D.C.'s are <math>\langle 0, \frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \rangle</math></p>	1
Question 14.	If $P(A) = \frac{3}{5}$ and $P(B) = \frac{1}{5}$ , find $P(A \cap B)$ if A and B are independent events.	
<b>Solution:</b>	<p>Since A and B are independent therefore <math>P(A \cap B) = P(A) \cdot P(B)</math></p> $\therefore P(A \cap B) = \frac{3}{5} \times \frac{1}{5} = \frac{3}{25}$	1
Question 15.	$\vec{a}$ and $-\vec{a}$ are collinear. (True / False)	
<b>Solution:</b>	True	1
Question 16.	The probability of obtaining an even prime number on each die, when a pair of dice is rolled is $\frac{6}{36}$ . (True / False)	
<b>Solution:</b>	<b>False</b>	1
Question 17.	If A and B are any two events such that $P(A) + P(B) - P(A \cap B) = P(A)$ , then $P(A B)$ _____.	
<b>Solution:</b>	<b>1</b>	1
Question 18.	The projection vector of $\vec{a} = \hat{i} + 3\hat{j} + 7\hat{k}$ on $\vec{b} = 7\hat{i} - \hat{j} + 8\hat{k}$ is _____.	









	<p>Since <math>xy = yx</math> This shows that R is reflexive.</p> <p>Further, <math>(x, y) R (u, v)</math>  <math>\Rightarrow xv = yu</math>  <math>\Rightarrow uy = vx</math>  <math>\Rightarrow (u, v) R (x, y)</math> <span style="float: right;"><math>\forall (x, y), (u, v) \in A</math></span>  This shows that R is symmetric.</p> <p>Similarly, <math>(x, y) R (u, v)</math> and <math>(u, v) R (a, b)</math>  <math>\Rightarrow \quad xv = yu \quad \text{and} \quad ub = va</math>  <math>\Rightarrow \quad \frac{x}{y} = \frac{u}{v} \quad \text{and} \quad \frac{u}{v} = \frac{a}{b}</math>  <math>\Rightarrow \quad \frac{x}{y} = \frac{a}{b}</math>  <math>\Rightarrow \quad xb = ya</math> <span style="float: right;"><math>\forall (x, y), (u, v), (a, b) \in A</math></span>  Hence <math>(x, y) R (a, b)</math>  Thus, R is transitive.  Thus, R is an equivalence relation.</p>	<p>1</p> <p>1</p> <p>1</p>
<p><b>OR</b> <b>Question 26.</b></p>	<p>Prove that: <math>\cos^{-1} \frac{12}{13} + \sin^{-1} \frac{3}{5} = \sin^{-1} \frac{56}{65}</math></p>	
<p><b>Solution:</b></p>	<p><math>\cos^{-1} \frac{12}{13} + \sin^{-1} \frac{3}{5} = \sin^{-1} \frac{56}{65}</math>  We know <math>\cos^{-1} x = \sin^{-1} \sqrt{1 - x^2}</math> <span style="float: right;">where <math>x &lt; 1</math></span>  <math>\Rightarrow \cos^{-1} \frac{12}{13} = \sin^{-1} \sqrt{1 - \left(\frac{12}{13}\right)^2}</math>  <math>\Rightarrow \quad \quad \quad = \sin^{-1} \sqrt{\frac{25}{169}}</math>  <math>\Rightarrow \cos^{-1} \frac{12}{13} = \sin^{-1} \frac{5}{13}</math>  Now taking L.H.S. <math>= \sin^{-1} \frac{5}{13} + \sin^{-1} \frac{3}{5}</math>  We know that,  <math>\sin^{-1} x + \sin^{-1} y = \sin^{-1} [x\sqrt{1 - y^2} + y\sqrt{1 - x^2}]</math> <span style="float: right;">if <math>xy &lt; 1</math></span>  <math>\therefore \quad \quad \quad = \sin^{-1} \left[ \frac{5}{13} \sqrt{1 - \left(\frac{3}{5}\right)^2} + \right.</math>  <math>\left. \frac{3}{5} \sqrt{1 - \left(\frac{5}{13}\right)^2} \right]</math>  <math>= \sin^{-1} \left[ \frac{5}{13} \sqrt{\frac{16}{25}} + \frac{3}{5} \sqrt{\frac{144}{169}} \right]</math>  <math>= \sin^{-1} \left[ \frac{5}{13} \left(\frac{4}{5}\right) + \frac{3}{5} \left(\frac{12}{13}\right) \right] = \sin^{-1} \frac{56}{65}</math>  L.H.S. = R.H.S.</p>	<p>1</p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p>







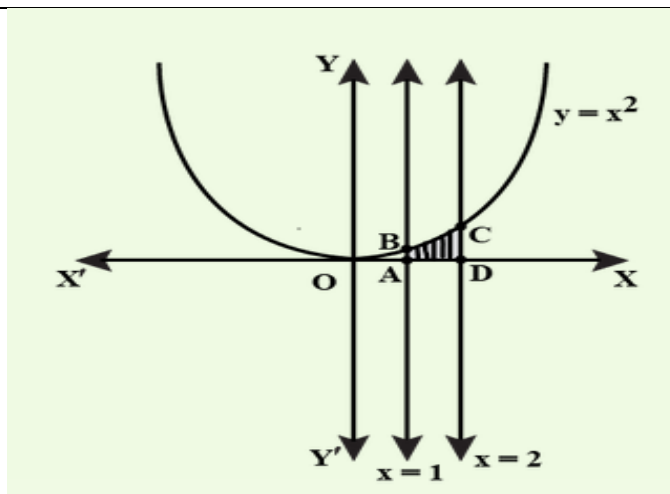
	<p>Here form of integral is <math>\int \frac{px+q}{\sqrt{ax^2+bx+c}} dx</math></p> <p><math>\therefore 4x + 1 = A \frac{d}{dx}(2x^2 + x - 3) + B</math></p> <p><math>4x + 1 = A(2x + 1) + B \quad \dots(1)</math></p> <p>On comparing the like terms , we have</p> <p><math>2A = 4</math> and <math>A + B = 1</math></p> <p><math>\Rightarrow A = 2</math> and <math>B = -1</math></p> <p><math>\Rightarrow 4x + 1 = 2(4x + 1) - 1 \quad \dots\text{from (1)}</math></p> <p><math>I = \int \frac{2(4x+1)-1}{\sqrt{2x^2+x-3}} dx</math></p> <p><math>I = 2 \int \frac{4x+1}{\sqrt{2x^2+x-3}} dx - \int \frac{1}{\sqrt{2x^2+x-3}} dx</math></p> <p>Put <math>2x^2 + x - 3 = t \Rightarrow (4x + 1) dx = dt</math></p> <p><math>I = 2 \int \frac{1}{\sqrt{t}} dt - \frac{1}{\sqrt{2}} \int \frac{1}{\sqrt{x^2 + \frac{1}{2}x - \frac{3}{2}}} dx</math></p> <p><math>I = 4\sqrt{t} - \frac{1}{\sqrt{2}} \int \frac{1}{\sqrt{x^2 + \frac{1}{2}x - \frac{3}{2}}} dx</math></p> <p><math>I = 4\sqrt{2x^2 + x - 3} - \frac{1}{\sqrt{2}} \int \frac{1}{\sqrt{x^2 + \frac{1}{2}x + \frac{1}{4} - \frac{1}{4} - \frac{3}{2}}} dx \quad (\text{completing the square})</math></p> <p><math>I = 4\sqrt{2x^2 + x - 3} - \frac{1}{\sqrt{2}} \int \frac{1}{\sqrt{(x + \frac{1}{2})^2 - (\frac{\sqrt{7}}{4})^2}} dx</math></p> <p><math>I = 4\sqrt{2x^2 + x - 3} - \frac{1}{\sqrt{2}} \log \left  \left(x + \frac{1}{2}\right) + \sqrt{\left(x + \frac{1}{2}\right)^2 - \left(\frac{\sqrt{7}}{4}\right)^2} \right  + C</math></p> <p><math>I = 4\sqrt{2x^2 + x - 3} - \frac{1}{\sqrt{2}} \log \left  \frac{(2x+1) + \sqrt{2x^2+x-3}}{2} \right  + C</math></p>	<p>1</p> <p>1</p> <p>1</p>
<p><b>OR</b> <b>Question 30.</b></p>	<p>Evaluate: <math>\int_2^8  x - 5  dx</math></p>	
<p><b>Solution:</b></p>	<p><math>I = \int_2^8  x - 5  dx</math></p> <p>We know <math> x - 5  = \begin{cases} -(x - 5), &amp; x \leq 5 \\ (x - 5), &amp; x &gt; 5 \end{cases}</math></p> <p><math>I = \int_2^5  x - 5  dx + \int_5^8  x - 5  dx</math></p> <p><math>I = \int_2^5 -(x - 5) dx + \int_5^8 (x - 5) dx</math></p>	<p><math>\frac{1}{2}</math></p>





	$\vec{a}_1 = -\hat{i} - \hat{j} - \hat{k}, \quad \text{and} \quad \vec{b}_1 = 7\hat{i} - 6\hat{j} + \hat{k}$ $\vec{a}_2 = 3\hat{i} + 5\hat{j} + 7\hat{k} \quad \text{and} \quad \vec{b}_2 = \hat{i} - 2\hat{j} + \hat{k}$ <p>Therefore <math>\vec{a}_2 - \vec{a}_1 = 4\hat{i} + 6\hat{j} + 8\hat{k}</math></p> <p>And <math>\vec{b}_1 \times \vec{b}_2 = (7\hat{i} - 6\hat{j} + \hat{k}) \times (\hat{i} - 2\hat{j} + \hat{k})</math></p> $= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 7 & -6 & 1 \\ 1 & -2 & 1 \end{vmatrix} = -4\hat{i} - 6\hat{j} - 8\hat{k}$ $ \vec{b}_1 \times \vec{b}_2  = \sqrt{16 + 36 + 64} = \sqrt{116}$ <p>Hence, the shortest distance between the given lines is given by</p> $D = \frac{ (\vec{a}_2 - \vec{a}_1) \cdot (\vec{b}_1 \times \vec{b}_2) }{ \vec{b}_1 \times \vec{b}_2 } = \frac{ (4\hat{i} + 6\hat{j} + 8\hat{k}) \cdot (-4\hat{i} - 6\hat{j} - 8\hat{k}) }{\sqrt{116}}$ $\frac{ -16 - 36 - 64 }{\sqrt{116}} = \frac{116}{\sqrt{116}} = \sqrt{116} = 2\sqrt{29}$	<p><math>\frac{1}{2}</math></p> <p>1</p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p>1</p>
<p><b>OR</b> <b>Question 33.</b></p>	<p>Find the vector equation of the line passing through the point <math>(1, -2, -3)</math> and perpendicular to the two lines : <math>\frac{x-1}{1} = \frac{y-2}{-1} = \frac{z-1}{3}</math> and <math>\frac{x-2}{2} = \frac{y+1}{1} = \frac{z+1}{2}</math>.</p>	<p>1</p>
<p><b>Solution:</b></p>	<p>The vector equation of a line passing through a point with position vector <math>\vec{a}</math> and parallel to <math>\vec{b}</math> is <math>\vec{r} = \vec{a} + \lambda \vec{b}</math>.</p> <p>It is given that, the line passes through <math>(1, -2, -3)</math> So, <math>\vec{a} = 1\hat{i} - 2\hat{j} - 3\hat{k}</math></p> <p>Given lines are <math>\frac{x-1}{1} = \frac{y-2}{-1} = \frac{z-1}{3}</math> and <math>\frac{x-2}{2} = \frac{y+1}{1} = \frac{z+1}{2}</math></p> <p>It is also given that, line is perpendicular to both given lines. So we can say that the line is perpendicular to both parallel vectors of two given lines.</p>	<p>1</p>

	<p>We know that, <math>\vec{a} \times \vec{b}</math> is perpendicular to both <math>\vec{a}</math> &amp; <math>\vec{b}</math>, so let <math>\vec{b}</math> is cross product of parallel vectors of both lines i.e. <math>\vec{b} = \vec{b}_1 \times \vec{b}_2</math>  where <math>\vec{b}_1 = \hat{i} - \hat{j} + 3\hat{k}</math> and <math>\vec{b}_2 = 2\hat{i} + \hat{j} + 2\hat{k}</math></p> <p>and Required Normal</p> $\vec{b} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -1 & 3 \\ 2 & 1 & 2 \end{vmatrix}$ $= \hat{i}(-2 - 3) - \hat{j}(2 - 6) + \hat{k}(1 + 2)$ $\vec{b} = -5\hat{i} + 4\hat{j} + 3\hat{k}$ <p>Now, by substituting the value of <math>\vec{a}</math> &amp; <math>\vec{b}</math> in the formula <math>\vec{r} = \vec{a} + \lambda \vec{b}</math>, we get</p> $\vec{r} = (1\hat{i} - 2\hat{j} - 3\hat{k}) + \lambda(-5\hat{i} + 4\hat{j} + 3\hat{k})$	<p>2</p> <p>1</p> <p>1</p>
<p><b>Question 34.</b></p>	<p>Find the area under the given curve <math>y = x^2</math> and the given lines <math>x = 1</math>, <math>x = 2</math> and x-axis.</p>	
<p><b>Solution:</b></p>	<p>Equation of the curve is <math>y = x^2</math>.  It is an upward parabola having vertex at origin and symmetrical about y-axis. <math>x = 1</math> and <math>x = 2</math> are two straight lines parallel to y-axis.  <math>y = x^2</math> ....(1) <math>x = 1</math> and <math>x = 2</math></p> <p>Points of intersections of given curves  At <math>x = 1</math>, <math>y = 1</math> points are (1, 1)  At <math>x = 2</math>, <math>y = 4</math> points are (2, 4)  ∴ Points in first quadrant A(1, 1) B(2, 4)  Points on x- axis with given lines are (1, 0) and (2, 0)</p> <p>Make a rough hand sketch of given curves by taking some corresponding values of x and y.</p>	<p><math>\frac{1}{2}</math></p> <p><math>1\frac{1}{2}</math></p>



Required area is shaded region ABCD:

$$|\int_1^2 y \, dx| = |\int_1^2 x^2 \, dx| \quad [ \text{From equation (1)} ]$$

$$= \left| \frac{x^3}{3} \right|_1^2$$

$$= \frac{1}{3} |(2^3 - 1^3)|$$

$$= \frac{1}{3} |(8 - 1)| = \frac{1}{3} (7) = \frac{7}{3} \text{ sq. units}$$

1

2

**OR**  
**Question 34.**

Find the area of the region bounded by the ellipse  $\frac{x^2}{4} + \frac{y^2}{9} = 1$

**Solution:**

$$\text{Here } \frac{x^2}{4} + \frac{y^2}{9} = 1 \quad \dots(1)$$

It is a vertical ellipse having center at origin and is symmetrical about both axes (if we change  $y$  to  $-y$  or  $x$  to  $-x$ , equation remain same).

$$\text{Standard equation of an ellipse is } \frac{x^2}{b^2} + \frac{y^2}{a^2} = 1$$

By comparing,  $a = 3$  and  $b = 2$

From equation (1)

$$\Rightarrow y^2 = \frac{9}{4} (4 - x^2)$$

$$\Rightarrow y = \frac{3}{2} \sqrt{4 - x^2} \quad \dots(2)$$

Points of Intersections of ellipse (1) with x-axis ( $y = 0$ )

Put  $y = 0$  in equation (1), we have

$\frac{1}{2}$

1

$$x^2/4 = 1 \Rightarrow x^2 = 4$$

$$\Rightarrow x = \pm 2$$

Therefore, Intersections of ellipse(1) with x-axis are (0, 2) and (0, -2).

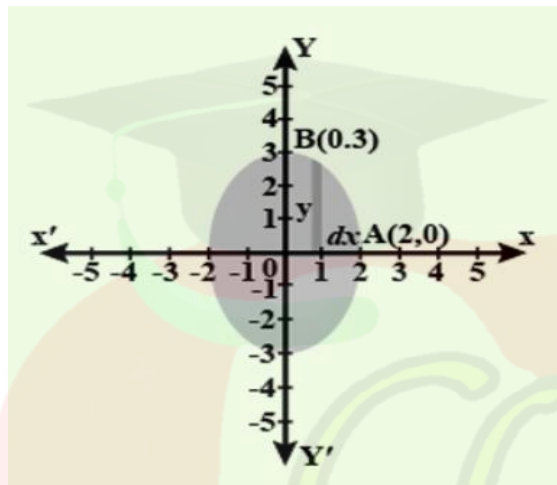
Points of Intersections of ellipse (1) with y-axis (x = 0)

$$\text{Putting } x = 0 \text{ in equation (1), } y^2/9 = 1 \Rightarrow y^2 = 9$$

$$\Rightarrow y = \pm 3.$$

Therefore, Intersections of ellipse (1) with y-axis are (0, 3) and (0,-3).

for arc of ellipse in first quadrant.



Now,

Area of region bounded by ellipse (1)

Total shaded area = 4 x Area OAB of ellipse in first quadrant

$$= 4 \left| \int_0^2 y \cdot dx \right| \quad [ \because \text{at end B of arc AB of ellipse: } x=0 \text{ and at end A of arc AB; } x=2 ]$$

$$= 4 \left| \int_0^2 \frac{3}{2} \sqrt{4 - x^2} \cdot dx \right| = 6 \left| \int_0^2 \sqrt{2^2 - x^2} \cdot dx \right|$$

$$= 6 \left[ \frac{x}{2} \sqrt{2^2 - x^2} + \frac{2^2}{2} \sin^{-1} \frac{x}{2} \right]_0^2 \quad [ \because \int \sqrt{a^2 - x^2} dx = \frac{x}{2} \sqrt{a^2 - x^2} + \frac{a^2}{2} \sin^{-1} \frac{x}{a} ]$$

$$= 6 \left[ \left( \frac{2}{2} \sqrt{4 - 4} + 2 \sin^{-1} 1 \right) - (0 + 2 \sin^{-1} 0) \right] = 6 \left[ 0 + \left( 2 \frac{\pi}{2} \right) \right]$$

$$= 6\pi \text{ sq. Units}$$

1

1/2

1 1/2

1/2



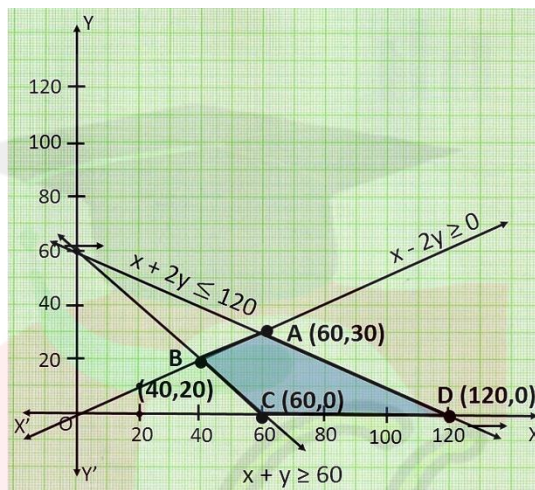
<b>Question 35.</b>	<p>Solve the following problem graphically:          Minimise and Maximise <math>Z = 5x + 10y</math>          Subject to the constraints: <math>x + 2y \leq 120</math>  <math>x + y \geq 60</math>  <math>x - 2y \geq 0</math>  <math>x \geq 0, y \geq 0</math></p>																	
<b>Solution:</b>	<p> <math>Z = 5x + 10y.</math> ... (1)  <math>x + 2y \leq 120</math> ... (2)  <math>x + y \geq 60.</math> ... (3)  <math>x - 2y \geq 0</math> ... (4)  <math>x \geq 0, y \geq 0</math> ... (5)         </p> <p>First of all, let us graph the feasible region of the system of linear inequalities (2) to (5).          Let <math>Z = 5x + 10y</math> ... (1)          Converting inequalities to equalities  <math>x + 2y = 120</math></p> <table border="1" data-bbox="331 968 581 1052"> <tr> <td>X</td> <td>0</td> <td>120</td> </tr> <tr> <td>Y</td> <td>60</td> <td>0</td> </tr> </table> <p>Points are (0, 60), (120, 0)</p> <p>Now put (0, 0) in inequation (2),          we find <math>0 \leq 120</math>, which is true.          Therefore area lies towards the origin from this line.</p> <p><math>x + y = 60</math></p> <table border="1" data-bbox="331 1392 581 1476"> <tr> <td>x</td> <td>0</td> <td>60</td> </tr> <tr> <td>y</td> <td>60</td> <td>0</td> </tr> </table> <p>Points are (0, 60), (60, 0)</p> <p>Now put (0, 0) in inequation (3),          we find <math>0 \geq 60</math>, which is False.          Therefore area lies away from the origin from this line.</p> <p><math>x - 2y = 0</math></p> <table border="1" data-bbox="331 1839 574 1881"> <tr> <td>X</td> <td>0</td> <td>20</td> <td>40</td> </tr> </table>	X	0	120	Y	60	0	x	0	60	y	60	0	X	0	20	40	<p style="text-align: center;"><math>\frac{1}{2}</math></p> <p style="text-align: center;"><math>\frac{1}{2}</math></p>
X	0	120																
Y	60	0																
x	0	60																
y	60	0																
X	0	20	40															

y	0	10	20
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Points are (0,0),(20,10),(40,20)  
 Now put (1, 0) in inequation (4),  
 we find  $1 \geq 0$ , which is true.  
 Therefore area lies towards (1, 0) origin from this line.

$\frac{1}{2}$

Plot the graph for the set of points



1

To find maximum and minimum  
 The feasible region ABCD is shown in the figure. Note that the region is bounded. The coordinates of the corner points A, B, C and D are (60, 30), (40, 20), (60, 0) and (120, 0) respectively.

$\frac{1}{2}$

Corner Point	Corresponding Value of $Z = 5x + 10y$
A (60, 30)	<b>600 ← Maximum</b>
B (40, 20)	<b>400</b>
C (60, 0)	<b>300 ← Minimum</b>
D (120, 0)	<b>600 ← Maximum</b>  (Multiple optimal solutions)

$1\frac{1}{2}$

We now find the minimum and maximum value of Z.  
 From the table, we find that the minimum value of Z is 300 at the point B (60, 0) of the feasible region.

	The maximum value of Z on the feasible region occurs at the two corner points C (60, 30) and D (120, 0) and it is 600 in each case.	$\frac{1}{2}$
	<b>SECTION – E ( 4Marks × 3Q)</b>	
<b>Question 36.</b>	<p><math>P(x) = -6x^2 + 120x + 25000</math> ( in ₹ ) is the total profit function of a company, where x denotes the production of the company.</p> <p><b>Based on the above information answer the following:</b></p> <p>(i) Find the profit of the company when the production is 3units. (1)</p> <p>(ii) Find <math>P'(5)</math>. (1)</p> <p>(iii) Find the production, when the profit is maximum. (2)</p>	
<b>Solution:</b>	<p>(i) When <math>x = 3</math>  <math>P(3) = -6(3)^2 + 120(3) + 25000</math>  <math>= -54 + 360 + 25000</math>  <math>= ₹ 25306</math></p>	1
	<p>(ii) We have, <math>P(x) = -6x^2 + 120x + 25000</math> ... (1)  Differentiating equation (1) w.r.t. x  <math>P'(x) = -12x + 120</math> ... (2)  <math>\therefore P'(5) = -12(5) + 120 = 60</math></p>	1
	<p>(iii) We have, <math>P(x) = -6x^2 + 120x + 25000</math> ... (1)  Differentiating equation (1) w.r.t. x  <math>P'(x) = -12x + 120</math> ... (2)  For maximum or minimum value of <math>P(x)</math>, <math>P'(x) = 0</math> we have  <math>-12x + 120 = 0</math>  <math>-12x = -120</math>  i.e. <math>x = 10</math>  Differentiating equation (2) w.r.t. x  <math>P''(x) = -12</math>  Now ,  At <math>x = 10</math> <math>P''(x) = -12 = -ve</math>  <math>\Rightarrow P(x)</math> has maximum value at <math>x = 10</math></p>	2
<b>Question 37.</b>	<p>A linear differential equation is of the form <math>\frac{dy}{dx} + Py = Q</math>, where P, Q are functions of x, then such equation is known as linear differential equation. Its solution is given by  <math>y \cdot (IF.) = \int Q(IF.) dx + c</math>, where I.F.( Integrating Factor) = <math>e^{\int P dx}</math>  Now, suppose the given equation is <math>x \frac{dy}{dx} + 2y = x^2</math>  Based on the above information, answer the following questions:</p>	

	<p>(i)What are the values of P and Q respectively? (1)</p> <p>(ii)What is the value of I.F.? (1)</p> <p>(iii)Find the Solution of given equation. (2)</p>	
<b>Solution:</b>	<p>(i) Given equation is <math>x \frac{dy}{dx} + 2y = x^2</math>  Dividing on both side by x, we have  <math display="block">\frac{dy}{dx} + \frac{2}{x}y = x</math>  <math display="block">\Rightarrow P = \frac{2}{x}, Q = x</math></p>	1
	<p>(ii) I.F.( Integrating Factor) = <math>e^{\int Pdx}</math>  <math display="block">= e^{\int \frac{2}{x}dx}</math>  <math display="block">= e^{2\log x}</math>  <math display="block">= x^2</math></p>	1
	<p>(iii) Solution of given equation is  <math display="block">y.(IF.) = \int Q(IF.) dx + c</math>  <math display="block">y(x^2) = \int x(x^2) dx + c</math>  <math display="block">x^2y = \int x^3 dx + c</math>  <math display="block">x^2y = \frac{x^4}{4} + c</math></p>	2
<b>Question 38.</b>	<p>In an office three employees Vinay, Sonia and Iqbal process incoming copies of a certain form. Vinay process 50% of the forms. Sonia processes 20% and Iqbal the remaining 30% of the forms. Vinay has an error rate of 0.06, Sonia has an error rate of 0.04 and Iqbal has an error rate of 0.03.  <i>Based on the above information answer the following questions:</i></p>	

	<p>(i) The total probability of committing an error in processing the form. (2)</p> <p>(ii) The manager of the company wants to do a quality check. During inspection he selects a form at random from the days output of processed forms. If the form selected at random has an error, the probability that the form is not processed by Vinay. (2)</p>	
<p><b>Solution:</b></p>	<p>(i) Let <math>E_1</math> = Event of processing form by Vinay.  <math>E_2</math> = Event of processing form by Soniya.  <math>E_3</math> = Event of processing form by Iqbal.</p> $P(E_1) = \frac{50}{100} = \frac{5}{10}, \quad P(E_2) = \frac{20}{100} = \frac{2}{10}, \quad P(E_3) = \frac{30}{100} = \frac{3}{10}$ <p>Also  <math>P(A/E_1) = 0.06, \quad P(A/E_2) = 0.04, \quad P(A/E_3) = 0.03</math></p> <p>Required Probability</p> $P(A) = P(E_1) \cdot P(A/E_1) + P(E_2) \cdot P(A/E_2) + P(E_3) \cdot P(A/E_3)$ $= \frac{5}{10} (0.06) + \frac{2}{10} (0.04) + \frac{3}{10} (0.03)$ $= 0.03 + 0.008 + 0.009 = 0.047$	<p>2</p>
	<p>(ii) Probability that the form is not processed by Vinay = <math>P(\bar{E}_1   A)</math>  <math>P(\bar{E}_1   A) = 1 - P(E_1   A)</math></p> <p>By Bayes' Theorem</p> $P(E_1   A) = \frac{P(E_1) \cdot P(A/E_1)}{P(E_1) \cdot P(A/E_1) + P(E_2) \cdot P(A/E_2) + P(E_3) \cdot P(A/E_3)}$ $P(E_1   A) = \frac{\frac{5}{10} (0.06)}{0.047}$ $P(E_1   A) = \frac{0.03}{0.047} = \frac{30}{47}$ $P(\bar{E}_1   A) = 1 - P(E_1   A)$ $= 1 - \frac{30}{47} = \frac{17}{47}$	<p>2</p>